

# Time delay observable in classical and quantum geometries

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100 years after Einstein, Prague

# Motivation

If I had a theory of Quantum Gravity, what would I do with it?

- ▶ Answer should be independent of QG model.
- ▶ **My answer:** Compute qualitative and quantitative QG corrections to experiments and observations.
- ▶ Unfortunately, what is easiest to compute in QG is model dependent may not have a direct experimental interpretation.
- ▶ **Idea:** Work backwards! Start with a potential experiment (even if only in principle possible), described operationally. Construct a mathematical model of it and obtain an observable quantity with an unambiguous interpretation.

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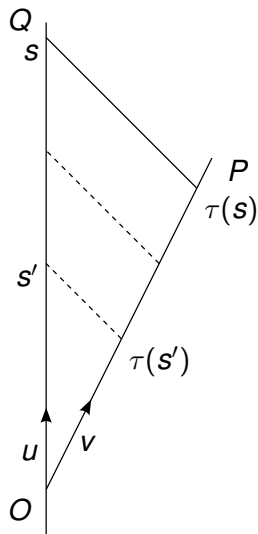
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# Time Delay Observable

operational definition



- ▶ Consider two inertially moving, localized systems: the **lab** and the **probe**. Probe is launched from the lab at event  $O$ .
- ▶ Each carries a **proper-time** clock. The clocks are synchronized at  $O$ .
- ▶ The probe broadcasts signals time stamped with the **emission time**,  $\tau$  at  $P$ .
- ▶ The lab records the **reception time**,  $s$  at  $Q$ , together with the time stamp  $\tau(s)$ .
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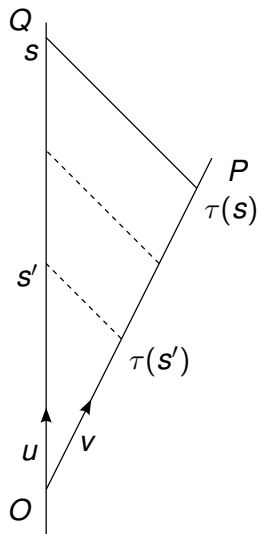
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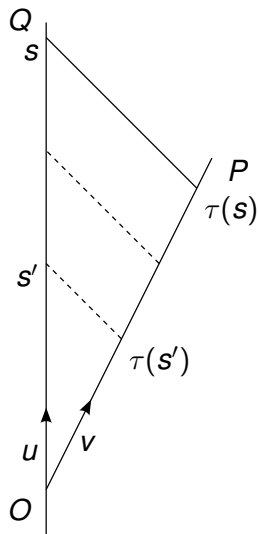
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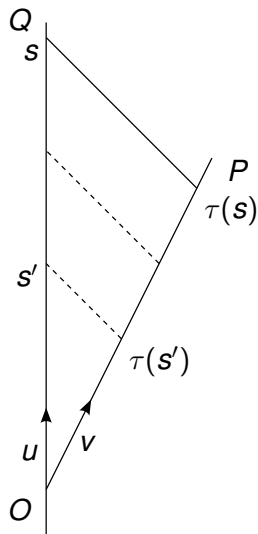
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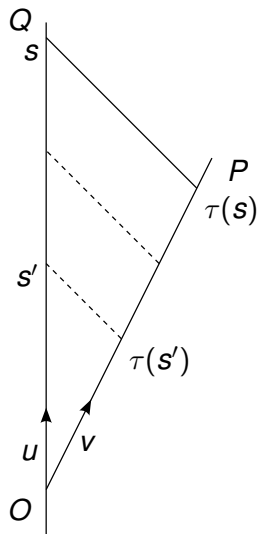
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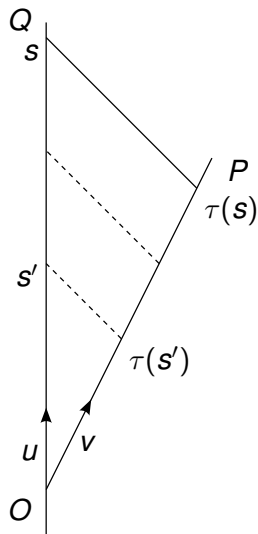
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- ▶ **Linearization** about Minkowski space:  $g_{\mu\nu} \rightarrow \eta_{\mu\nu} + h_{\mu\nu}$ .
- ▶ **Quantization** as linearized field theory:  $h_{\mu\nu} \rightarrow \hat{h}_{\mu\nu}$ .
- ▶ **Explicit** expression for  $\tau(s)$  at order  $O(h)$  is available:

$$\begin{aligned}\tau(s) &= \tau[\eta](s) + \tau_1[h](s) + \dots \\ &= s e^{-\theta} (1 + r[h] + \dots) \\ r[h] &= r^X h_X = H + J\end{aligned}$$

- ▶  $\theta$ —rapidity,  $v_{\text{rel}} = \tanh(\theta)$
- ▶  $r^X$ —integro-differential operator
- ▶  $H, J$ —separately **invariant** under linearized diffeomorphisms that fix  $O$  and  $e^\alpha$
- ▶ **Note:**  $H, J, \dots$  may have been found by brute force, but it would not have been obvious how these **invariants** would combine into an **observable** with direct **phenomenological interpretation**

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# Explicit Calculation

## basic idea

- ▶ Vacuum  $|0\rangle$  is Gaussian wrt  $\hat{\tau}$ , with mean  $\tau_{\text{cl}}$ . Remains to compute variance:  $\langle(\Delta\hat{\tau})^2\rangle = \langle\hat{\tau}^2\rangle - \langle\tau\rangle^2 = \tau_{\text{cl}}\langle\hat{\tau}^2\rangle$ , with  $\hat{r} = r[\hat{h}] = r^x\hat{h}_x$ .
- ▶ Variance needs the **Hadamard** 2-point function  $G(x, y)$ .

$$\langle 0|\hat{r}^2|0\rangle = \frac{1}{2}\langle\{\hat{r}, \hat{r}\}\rangle = \frac{1}{2}r^x r^y \langle\{\hat{h}_x, \hat{h}_y\}\rangle = \frac{1}{2}r^x r^y G(x, y)$$

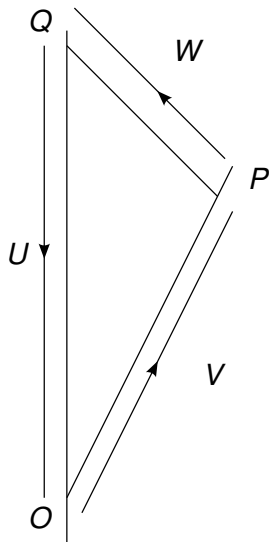
- ▶ Integrals in  $r^x$  are not sufficient to tame the  $x - y \rightarrow 0$  **divergence** of  $G(x, y) \sim \ell_p^2/(x - y)^2$ . Need to use **smeared** fields  $\tilde{h}$ :

$$\tilde{r} = r^x \tilde{h}_x = r^x \langle\langle \hat{h}_{x-z} \rangle\rangle,$$
$$\langle\langle f(z) \rangle\rangle = \int dz f(z) \tilde{g}(z),$$

where  $\tilde{g}(z)$  is a **smearing function**, localized at  $z = 0$ , of spread  $\mu \ll s$ :  $\langle\langle z^n \rangle\rangle \sim \mu^n$ .

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explicit expressions



$$r^x h_x = H + J$$

► Explicit expression:

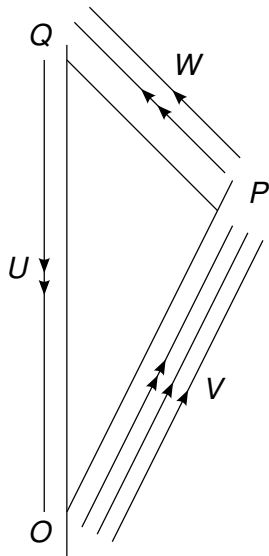
$$H \sim \sum_{X=V,U,W} (\longrightarrow)_X,$$

$$(\longrightarrow)_X \sim \int_X^{(1)} \nabla h.$$

►  $H$  is invariant under linearized diffeomorphisms that fix  $O$  and  $e^\alpha$ .

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$$r^x h_x = H + J$$

► **Explicit** expression:

$$J \sim \sum_{X=V,U,W} \left[ (\longrightarrow)_{\rightarrow X} + \sum_{Y < X} (\longrightarrow)_{\rightarrow Y} \right],$$

$$(\longrightarrow)_{\rightarrow X} \sim \int_X^{(1)} h + \int_X^{(2)} \nabla h,$$

$$(\longrightarrow)_{\rightarrow Y} \sim \int_Y^{(1)} \nabla h.$$

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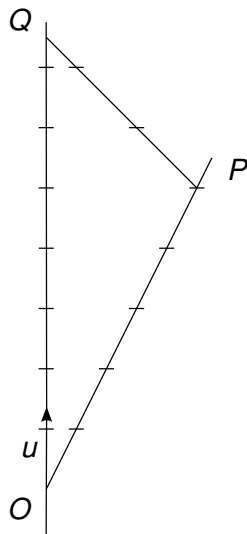
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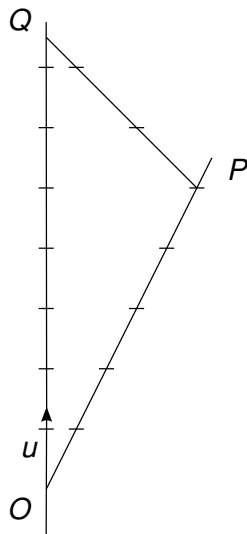
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# Smearing and Detector Resolution



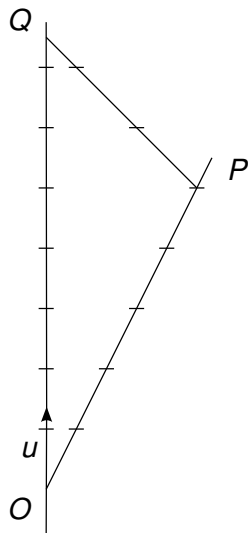
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- ▶ Physically speaking,  $\mu$ , the spread of  $\tilde{g}(x)$ , is the **spatial resolution** of the detector.
- ▶ We can back-of-envelope **estimate**  $\mu$  as the **wavelength** of the light/radio signals exchanged between lab and probe.
- ▶ A more detailed detector model should unambiguously fix  $\tilde{g}(x)$  for each leg of  $\triangle OPQ$ .
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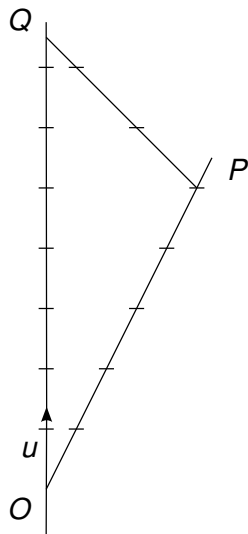
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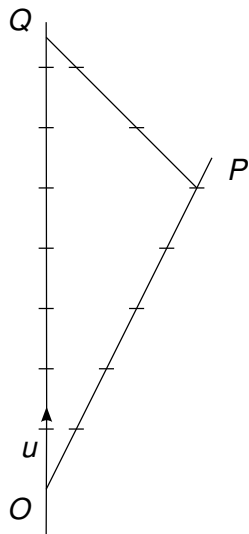


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# Explicit Calculation

## dimensional analysis

- Dimensional analysis:  $[\mu] = [\ell_p] = [z] = 1$ ,  $[\nabla] = -1$ ,  $G \sim \ell_p^2/z^2$ .

$$\begin{aligned}\langle \tilde{r}^2 \rangle &\sim s^2 \left\langle \int_X \int_Y \nabla^2 G(z) \right\rangle \sim s^2 \left\langle \int_X \int_Y \frac{\ell_p^2}{z^4} \right\rangle \\ &\sim s^2 \left\langle \frac{\ell_p^2}{s^2 z^2} \right\rangle \sim \frac{\ell_p^2}{\mu^2}\end{aligned}$$

- Detailed calculations reveal terms like  $\frac{\ell_p^2}{\mu^2} \ln(s/\mu)$  and even  $\frac{s\ell_p^2}{\mu^3}$ .

- Expected rms fluctuation in  $\hat{\tau}(s) \sim s\sqrt{\langle \tilde{r}^2 \rangle} \sim s\frac{\ell_p}{\mu}$  or  $s\frac{s^{1/2}}{\mu^{1/2}}\frac{\ell_p}{\mu}$ .

$\mu \sim 1\text{nm}$  (X-rays)

laboratory:  $s \sim 1\text{m} \sim 10^{-9}\text{s}$ ,  $\frac{\ell_p}{\mu} \sim 10^{-26}$ ,  $\frac{s^{1/2}}{\mu^{1/2}} \sim 10^5$ :  $10^{-35}\text{s}$  or  $10^{-30}\text{s}$

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$\mu \sim 1\text{nm}$  (X-rays)

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# Explicit Calculation

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Thank you for your attention!