

V-band photometry of asteroids from ASAS-SN

Finding asteroids with slow spin*

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ABSTRACT

We present V-band photometry of the 20000 brightest asteroids using data from the All-Sky Automated Survey for Supernovae (ASAS-SN) between 2012 and 2018. We were able to apply the convex inversion method to more than 5000 asteroids with more than 60 good measurements in order to derive their sidereal rotation periods, spin axis orientations, and shape models. We derive unique spin state and shape solutions for 760 asteroids, including 163 new determinations. This corresponds to a success rate of about 15%, which is significantly higher than the success rate previously achieved using photometry from surveys. We derive the first sidereal rotation periods for additional 69 asteroids. We find good agreement in spin periods and pole orientations for objects with prior solutions. We obtain a statistical sample of asteroid physical properties that is sufficient for the detection of several previously known trends, such as the underrepresentation of slow rotators in current databases, and the anisotropic distribution of spin orientations driven by the nongravitational forces. We also investigate the dependence of spin orientations on the rotation period. Since 2018, ASAS-SN has been observing the sky with higher cadence and a deeper limiting magnitude, which will lead to many more new solutions in just a few years.

Key words. minor planets, asteroids: general – surveys – methods: observational – methods: data analysis

1. Introduction

A large number of sky surveys have monitored the sky with various depths, cadences, coverage areas, and scientific goals. Examples include the All-Sky Automated Survey (ASAS; Pojmanski 2002), the Optical Gravitational Lensing Experiment (OGLE; Udalski 2003), the Northern Sky Variability Survey (NSVS; Woźniak et al. 2004), MACHO (Alcock et al. 1997), EROS (Palanque-Delabrouille et al. 1998), the Catalina Sky Survey (CSS; Larson et al. 2003), the Asteroid Terrestrial-impact Last Alert System (ATLAS; Tonry et al. 2018), Gaia (Gaia Collaboration 2016), the Zwicky Transient Facility (ZTF; Bellm et al. 2019), Kepler (Borucki et al. 2010), TESS (Ricker et al. 2015), and PanSTARRS (Chambers et al. 2016). Although several surveys were designed specifically to find asteroids, most of them are not primarily dedicated to the study of Solar System bodies, but could be used to do so with some effort (e.g., Ďurech et al. 2020; Pál et al. 2020; Szabó et al. 2016: Gaia Collaboration 2018).

Long-term calibrated photometry from modern time-domain surveys both from the ground and from space has been an important tool for the physical characterization of Solar System bodies. For example, the Sloan Digital Sky Survey data revealed a bimodal distribution of the broadband colors of mainbelt asteroids caused by differences between rocky and carbonaceous surface compositions (Ivezić et al. 2001). Time series data from K2 (Szabó et al. 2016) and TESS (Pál et al. 2020) were used to determine rotation periods for a large number of asteroids.

The information content in the light curves is not limited to the rotation periods only. Durech et al. (2010) presented a database of asteroid rotation periods, pole orientations, and three-dimensional (3D) convex shapes determined using the photometry inversion technique of Kaasalainen & Torppa (2001) and Kaasalainen et al. (2001). There are currently (as of February 2021) 5715 shape models for 3303 asteroids,¹ and the number of solutions is continuously expanding as new data become available. For example, Durech & Hanuš (2018) and Durech et al. (2020) determined 3D convex shape models and rotation pole orientations for 129 and 1800 asteroids using Gaia DR2 and ATLAS photometry, respectively.

Understanding the distribution of spin vectors is important for constraining the evolution of asteroid rotational states. Hanuš et al. (2011, 2013a) identified the signatures of the

^{*} Full Tables A.1-A.4 are only available at the CDS via anonymous ftp to cdsarc.u-strasbg.fr (130.79.128.5) or via http: //cdsarc.u-strasbg.fr/viz-bin/cat/J/A+A/654/A48
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https://astro.troja.mff.cuni.cz/projects/damit/

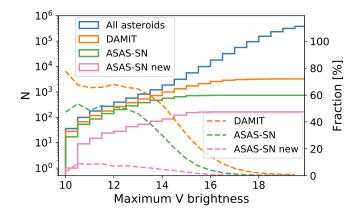


Fig. 1. Distributions of asteroids and available shape models as a function of maximum V-band magnitude. The solid lines show all known asteroids (blue), shape solutions available in the DAMIT database (orange), shape solutions obtained from ASAS-SN data in this work (green), and the asteroids with new shape models from this work (pink). The dashed lines show the percentage of all asteroids that have shape solutions.

thermal Yarkovsky–O'Keefe–Radzievskii–Paddack effect (YORP; Bottke et al. 2006), which pushes the spin orientation of smaller asteroids to align perpendicularly to their orbital planes. Even better constraints on individual asteroid properties can be obtained by combining shape modeling with infrared photometry (Hanuš et al. 2015, 2018; Ďurech et al. 2017), occultations of stars (Ďurech et al. 2011), adaptive optics imaging (Hanuš et al. 2013b, 2017; Viikinkoski et al. 2017, 2018; Vernazza et al. 2018), and interplanetary mission flybys (Preusker et al. 2016a,b, 2017; Watanabe et al. 2019).

Bright asteroids are often the most suitable targets for detailed studies, but the currently available data do not provide a complete picture of the asteroid population. In Fig. 1 we show the fraction of asteroids that have shape models as a function of their maximum V-band magnitude. We see that the completeness is about 70% at the bright end, and begins to decrease for V > 14 mag. More observations, even of bright asteroids, are needed.

In this paper we present V-band photometry of asteroids obtained with the All-Sky Automated Survey for Supernovae (ASAS-SN; Shappee et al. 2014; Kochanek et al. 2017) between the years 2012 and 2018. During this period ASAS-SN monitored the sky with a cadence of 2-3 days to a depth of $V \sim 17 \text{ mag}$ using two units in Chile and Hawaii. Although the primary goal of ASAS-SN is the hunt for supernovae (Holoien et al. 2017) and other transients such as tidal disruption events (Holoien et al. 2014) or novae (Aydi et al. 2020), it has been used much more broadly to, for example, characterize stellar variability (Jayasinghe et al. 2018, 2019, 2020b; Pawlak et al. 2019; Bredall et al. 2020) or even to discover comets (ASASSN1 or C/2017 O1 and ASASSN2 or C/2018 N2; Prieto et al. 2017; Brinkman 2020; van Buitenen et al. 2018). In this paper we use the calibrated ASAS-SN disk-integrated photometry for the physical characterization of asteroids, in terms of their sidereal rotation periods, spin axis orientation, and 3D shape models.

The structure of our paper is as follows. First, we describe our ASAS-SN data processing pipeline in Sect. 2. Then, we outline the light curve inversion scheme, apply it to ASAS-SN photometry, and derive physical properties for several hundred asteroids in Sect. 3. We discuss our results and derived physical properties in Sect. 4, and conclude our work in Sect. 5.

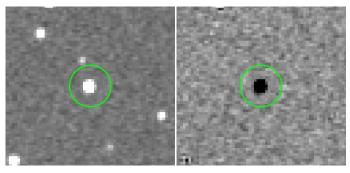


Fig. 2. Example of typical images obtained by ASAS-SN. *Left*: image containing asteroid (130) Elektra with an exposure time of 90 s. *Right*: corresponding subtracted image (reference image minus observation). The circle of 1 arcmin in radius is centered on the predicted coordinates of Elektra.

2. ASAS-SN V-band photometry

During 2012–2018 ASAS-SN consisted of two units in Chile and Hawaii. Each unit consisted of a robotic mount with four 14 cm telescopes each with a $4.5^{\circ} \times 4.5^{\circ}$ field of view. The detectors were 2048² cooled, back-illuminated CCDs with 8".0 pixels, and the image FWHM was roughly 2 pixels. During this period, the survey used a V filter with a typical limiting magnitude of $V \sim$ 17 mag under good sky conditions. This dataset is the focus of the paper. Since 2018 ASAS-SN has expanded to five units with new mounts in Chile, Texas, and South Africa, and switched to the Sloan g filter with a limiting magnitude of $g \sim$ 18.5 mag. These observations are continuing and will be the subject of a future work

Each ASAS-SN epoch consists of three (10 pixel) dithered images each with an exposure time of 90 s and roughly 15 s between exposures. The photometry is based on image subtraction followed by aperture photometry on the difference image. In image subtraction a reference image constructed by combining large numbers of high quality images is scaled in flux and PSF structure to match the new data, and is then subtracted to leave an image consisting only of the changes from the reference image (Alard & Lupton 1998; Alard 2000), see an example in Fig. 2. Because the reference image is built from a large number of images, its contribution to the statistical noise is negligible. Fields are observed to optimize the discovery of supernova-like transients based on the age and quality of the last observation. A particular field is visited only once per night. However, there is no fixed temporal spacing (see Fig. 2 in Pawlak et al. 2019), and in searches for variable stars, there is no difficulty with measuring periods of $\sim 1 \text{ hr}$ (Jayasinghe et al. 2020a,b). Only simple multiples of the diurnal period have significant power in the typical window function.

We performed the absolute calibration using the AAVSO Photometric All-Sky Survey (APASS; Henden et al. 2015) catalog. Ephemeris tables from Miriade accurately predict the location of asteroids in the ASAS-SN data. We selected a region around the predicted position, centered on the emission from the asteroid, and then measured the flux with aperture photometry.

Given the limiting magnitude of ~17, we decided to extract data for the first 10 000 numbered asteroids plus the remaining asteroids predicted to become brighter than V = 16.5 mag. In total, our initial dataset involves ~20 000 asteroid light curves. We show the basic statistics in Fig. 3. We have at least 10 flux measurements for ~19 000 asteroids, at least 100 for ~7000 asteroids, and at least 200 for ~1000 asteroids. The average

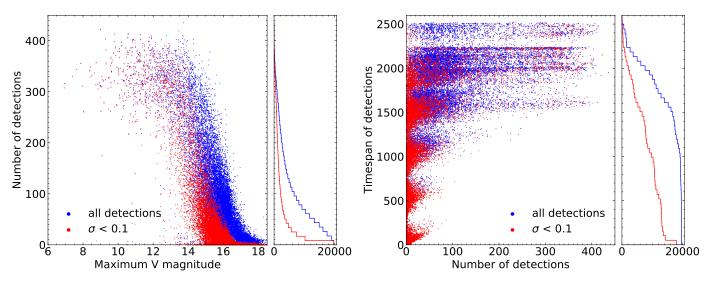


Fig. 3. Basic statistics of the ASAS-SN data. *Left*: number of individual detections for each asteroid as a function of the maximum *V*-band magnitude predicted by Miriade. *Right*: timespan of the observations in days as a function of the number of detections. Asteroids with average photometric uncertainties $\sigma < 0.1$ mag are shown in red.

photometric accuracy is <0.1 mag for about one-third of the objects. About 80% of the asteroids have data spanning more than 1500 days (4.1 yrs) corresponding to 3–5 apparitions for each asteroid. Having data from at least three different apparitions (i.e., different viewing geometries) is crucial for successful shape modeling by the light curve inversion technique (Kaasalainen et al. 2001).

Our data contain a significant fraction of clear outliers. To identify them, we use Miriade² to obtain the predicted *V*-band magnitude for each epoch. We remove points for which the extracted magnitude differs from the predicted by more than 0.7 magnitude. We selected this threshold because the predicted magnitude reflects the light curve average, while the observed magnitude can correspond to any part of the light curve. Light curve amplitudes (peak to peak) are rarely larger than one magnitude, so our threshold should be sufficiently generous to avoid rejecting real data even for asteroids with extreme amplitudes.

Our data processing follows the standard approach applied to sky survey data (e.g., Hanuš et al. 2011, 2013a; Ďurech et al. 2016, 2020; Ďurech & Hanuš 2018). First, we obtain the asterocentric ecliptic coordinates of the Sun and the Earth using Miriade. Having the distances of the asteroid from the Earth, we correct the epochs for light travel times. Then, we transform the magnitudes to intensities, defining a magnitude of 15 to correspond to an intensity of unity for later computational convenience. Next, we normalize the flux intensities to distance of 1 au (astronomical unit) from the Earth and the Sun and average them to unity. We fit the data with a standard phase function (Kaasalainen et al. 2001)

$$f(\alpha) = A_0 \exp \frac{-\alpha}{D} - k\alpha + 1, \tag{1}$$

where α is the phase angle and A_0 , D, k are free parameters, and then remove any remaining outliers using sigma clipping. We use a clipping threshold of 2.5 σ based on our empirical experience (also see Durech et al. 2020). In cases with a small number of data points (\leq 30) or a poor sampling of low phase angles ($\alpha < 10^\circ$) the fitting sometimes fails. For these cases we only use the linear part of the phase function for outlier rejection (i.e., we set $A_0 = 0$). As a final step, we keep only measurements with photometric accuracy better than 0.15 mag. This threshold is a reasonable compromise between including too much data with poor photometric quality and removing too many useful measurements. Typical ASAS-SN V-band data are illustrated in Fig. 4 for the main-belt asteroid (130) Elektra.

These steps rejected 30% of the data points on average. The losses were small for bright asteroids (<10% rejected for V < 15.5 mag), but significant for the fainter asteroids (often more than 40–50% for V > 16 mag). Our catalog of ASAS-SN V-band photometry for 19402 asteroids is presented in Table A.1. For each photometric data point we provide the Julian date, V-band magnitude with the uncertainty, and flags indicating whether the data point was used in the light curve inversion.

For the purpose of the shape modeling by the convex inversion algorithm (Sect. 3), calibrated photometry normalized to unity is sufficient because we only need relative changes of the brightness. The fit of the phase function by a semi-empirical model (Eq. (1)) is part of the convex inversion. Therefore, the possible prior conversion to the more common absolute magnitudes H_V was not needed. Anyone interested in H_V magnitudes can use our catalog of V-band magnitudes and can do the analysis of the phase function independently.

3. Determination of physical parameters by photometry inversion

In this section we describe the light curve inversion scheme we apply to the ASAS-SN *V*-band data in Sect. 3.1 and the threshold we use to evaluate the uniqueness of the solutions in Sect. 3.2. Finally, we derive new spin state and shape solutions in Sect. 3.3.

3.1. Inversion scheme

We applied the convex inversion (CI) of Kaasalainen & Torppa (2001) and Kaasalainen et al. (2001) to all asteroids with more than 60 individual measurements (5283 asteroids). This requirement reflects the minimum number of free parameters in the model (55): 49 for shape parameterization, 3 for rotation state (sidereal rotation period, orientation of the spin axis), and 3

² http://vo.imcce.fr/webservices/miriade/

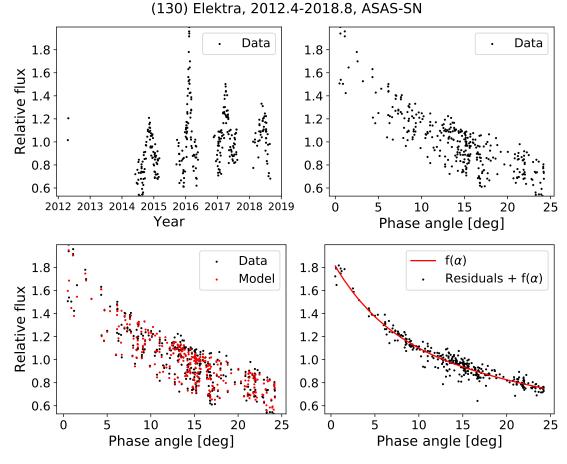


Fig. 4. Typical ASAS-SN *V*-band photometry. *Top row*: ASAS-SN normalized *V*-band photometry of asteroid (130) Elektra as a function of time (*left*) and phase angle α (*right*). *Bottom row*: comparison between the observed data and the model for asteroid (130) Elektra as a function of phase angle α (*left*) and the fit residuals with respect to the phase function $f(\alpha)$ (*right*). The actual H_V values are not relevant for our study, and therefore the relative flux is used instead.

phase function parameters (Eq. (1)). CI is a gradient-based inversion algorithm that converges to the nearest local minimum given the initial values of the rotation state parameters. We needed to run the minimization multiple times to ensure that we did not miss the global minimum. In practice, the shape modeling consists of four consecutive steps.

In the first step we scan the period interval of 2–1500 hrs. All the asteroids in our sample are large enough to be viewed as rubble piles that cannot rotate faster than the critical rotation period of ~2 hrs (Pravec & Harris 2000). Rotation periods longer than 1500 hours are extremely rare and difficult to derive even from sky-survey data. Moreover, these bodies likely rotate in the non-principle axis regime, which we cannot properly model by our method (Pravec et al. 2005). To find the true rotation period, we need to sample a parameter space that is densely filled with local minima. The difference between two local minima in the rotation period parameter space ΔP can be approximated as

$$\frac{\Delta P}{P} = \frac{1}{2} \frac{P}{T},\tag{2}$$

where *T* is the time span of the data (Kaasalainen et al. 2001). Therefore, we run the shape models for all periods in the 2–1500 h interval separated by $0.5\Delta P$. For each trial period, we run the shape models with ten different initial pole orientations, isotropically distributed on a sphere.

In the second step, if we find a single rotation period that fits the data significantly better than all the other period values, we run the convex inversion with this period and a finer grid for the initial pole orientations. Our chi-square threshold is defined by

$$\chi^2_{\rm tr} = \left(1 + p \sqrt{\frac{2}{\nu}}\right) \chi^2_{\rm min},\tag{3}$$

where χ^2_{\min} is the chi-square of the global minimum, ν is the number of degrees of freedom (number of observations minus the number of free parameters), and *p* is a weighting factor. We discuss the selection of *p* in Sect. 3.2.

In the third step, if we find one or two pole solutions that fit the data better than the remaining ones (again by using Eq. (3)), we use the convex inversion algorithm to obtain a unique solution with these poles and rotation period as starting values.

In the fourth step the shape model is represented by a set of areas and their normals (Kaasalainen & Torppa 2001), and the vertices (the shape is represented as a convex polyhedron) are computed using Minkowski minimization (Kaasalainen et al. 1992; Lamberg 1993).

As in Durech & Hanuš (2018) and Durech et al. (2020), we also use a simple tri-axial ellipsoidal model to scan the rotation period parameter space. These models are easily forced to be physical by requiring the semi-major axes to be a > b > c = 1. The convention is that *c* is the principal rotation axis that maximizes the moment of inertia. While convex inversion often results in similarly good fits for both the correct period *P* and its multiples, most commonly *P*/2, light curve inversion with

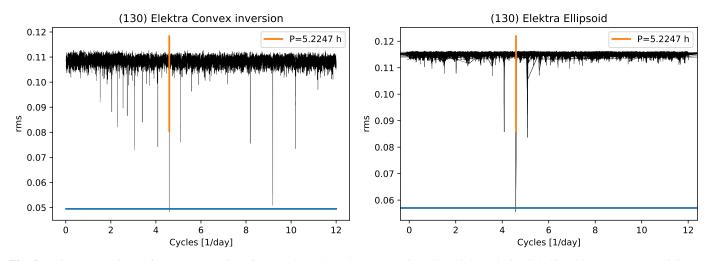


Fig. 5. Periodograms (in the frequency domain) of (130) Elektra based on convex inversion (*left*) and tri-axial ellipsoids (*right*). Each minimum represents one trial run sampling all the local minima at fixed rotation period. The vertical line indicates the best-fitting value (consistent with the LCDB period of 5.225 h). The horizontal line represents the χ^2 threshold defined by Eq. (3). There are more than 110 000 trial periods for Elektra (see Eq. (2)). The prominent side minima near *P* and *P*/2 are the aliases at ±0.5 cycles day⁻¹ around *P* and ±1 cycles day⁻¹ around *P*/2. Convex inversion models generically show more periodogram structure than the ellipsoidal models.

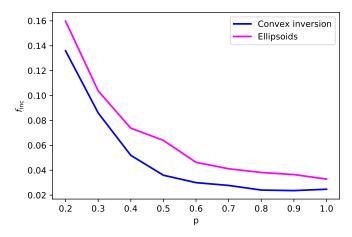


Fig. 6. Dependence of the false solution rate f_{inc} on the parameter p defined in Eq. (3) for both the convex inversion (blue) and tri-axial ellipsoid models (magenta).

tri-axial ellipsoids usually favors only the correct period P (see Fig. 5). Fortunately, convex inversion solutions with periods P/2 are often nonphysical because they also tend to force the principle rotation axis c to be the longest, which is nonphysical. We only use the ellipsoidal model for the rotation period and then compute the shape using the convex inversion method.

3.2. Period threshold

Our criterion for the uniqueness of the best-fitting rotation period is defined by Eq. (3), where we need to select the optimal value of the *p* factor. We do this using comparisons to the asteroid Lightcurve Database (LCDB; Warner et al. 2009) compilation of asteroid physical properties, including rotation periods. Each period is ranked by a flag that indicates its reliability. For our analysis we selected only the most reliable values with flags "3" and "3–". Figure 6 shows the fraction f_{inc} of the ASAS-SN periods that disagree with the previously reported values as a function of *p* for the two fitting methods. We omit cases where the LCDB period is twice the ASAS-SN period. For p < 0.5, f_{inc} increases rather rapidly. So we select p = 0.5 as an optimal value in the CI and p = 0.6 in the tri-axial ellipsoid shape analyses.

For these choices, about 3% of periods derived by ČI from ASAS-SN data are inconsistent with the LCDB periods. We discuss several individual cases in Sect. 3.3. It is important to keep in mind that not all flag 3 and 3- periods in LCDB will be correct. Ďurech et al. (2016, 2020) found multiple examples of incorrect estimates and f_{inc} on the order of a few percent is not particularly concerning. The incorrect periods were generally for asteroids with P > 20 h, where determinations are more challenging for classical short duration, dense sampling light curve observations. The f_{inc} ratio for the tri-axial ellipsoid approach is higher by about 2% than for the convex inversion approach. The minor increase is likely due to the ellipsoidal approach being less physically realistic.

We also see cases where the ASAS-SN period is clearly incorrect. For example, a few tens of the brightest asteroids have at least partly saturated photometry, which sometimes result in best-fitting period values of 24 or 48 h. We rejected these objects from our analysis. Additionally, we also identified cases with a relatively low number of detections (<100) and "suspicious" periodograms. Usually, good periodograms are qualitatively similar to the one of asteroid (130) Elektra (Fig. 5); most of these solutions cluster along the line of constant maximum rms and only several deep and sharp minima are present, usually in simple ratios. Suspicious periodograms have larger scatter and a more random distribution of minima. We also removed these solutions from our analysis. Finally, many solutions with inconsistent LCDB periods were rejected by our additional reliability tests.

We only accepted a solution if it had at most two pole solutions passing the statistical threshold of Eq. (3), and if the two poles were the so called mirror solutions (similar ecliptic latitude and an ecliptic longitude difference of ~180 degrees, Kaasalainen & Lamberg 2006). The shape solution also needed to be physically plausible, with the body rotating along its shortest axis. Therefore, we computed the axis with the maximum momentum of inertia of the body (Dobrovolskis 1996) and compared it with the position of the spin axis.

We evaluated the models using the dependence of the brightness on phase angle (Fig. 4) and rotation phase (Fig. 7), which

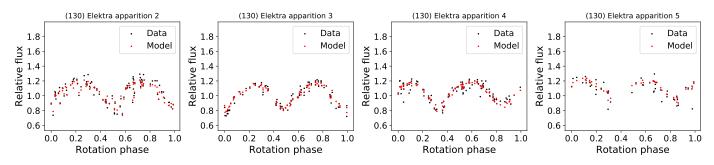


Fig. 7. Fit to the ASAS-SN data for asteroid (130) Elektra. The data is split into four apparitions and is shown as a function of rotation phase given the sidereal rotation period of 5.22466 h. The model for each apparition shows scatter because the geometry is also changing during each apparition. The phase reference time is defined independently for each apparition.

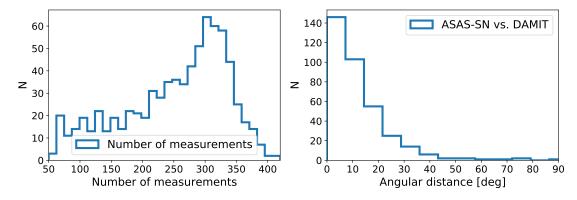


Fig. 8. Data amount and pole consistency for ASAS-SN solutions. *Left*: histogram of the number of ASAS-SN *V*-band measurements for the asteroids with successful shape solutions. *Right*: angular distance between the ASAS-SN and DAMIT pole solutions.

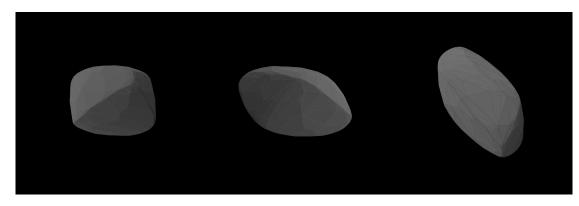


Fig. 9. First convex shape model of asteroid (1532) Inari. The left and center views are equatorial with a 90° rotation, while the right view is pole-on.

we illustrate using asteroid (130) Elektra. In both cases the mean brightness is normalized to unity. Because the geometry changes with apparition, the phase-folded light curves change with each apparition. The models for each apparition also show scatter due to changes in geometry during the individual apparitions. Similarly, the scatter in the data is a combination of the photometric errors and the changes in geometry. Moreover, the folded plots also illustrate the sufficient coverage of the rotation phase by the data and that the residuals are significantly smaller than the light curve amplitude.

3.3. New shape solutions from ASAS-SN data

From the 5283 asteroids with more than 60 photometric measurements, we derived unique spin state and shape solutions for

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760 asteroids. This corresponds to a success rate of about 15%, which is significantly higher than the success rate from the previous wide-area surveys such as ATLAS (~3%, Ďurech et al. 2020), *Gaia* DR2 (~3%, Ďurech & Hanuš 2018), and Lowell alone or in combination with WISE ($\leq 1\%$, Ďurech et al. 2016, 2018).

We obtained new shape model determinations for 163 individual asteroids. A typical example is shown in Fig. 9 (asteroid 1532 Inari). We list their physical properties in Table A.2. The solutions for asteroids with shape models already included in DAMIT are provided in Table A.3. Figure 8 compares our pole directions and those reported in DAMIT. The difference is rarely larger than 30° , which suggests a good consistency between our solutions and previous estimates. Additionally, we derived sidereal rotation periods for 69 asteroids for the first

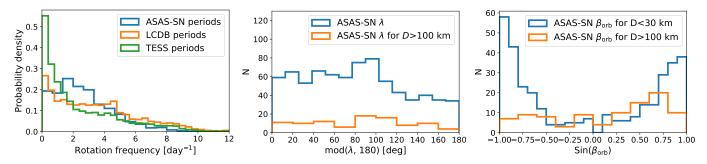


Fig. 10. Rotation period and pole direction distributions. *Left*: Normalized period distributions for the ASAS-SN models (760), TESS periods (9912, Pál et al. 2020), and LCDB periods (31 280, Warner et al. 2009). *Middle*: distribution of pole ecliptic longitudes λ for all asteroids and asteroids >100 km derived from the ASAS-SN data. *Right*: distribution of orbital pole latitudes β_{orb} derived from ASAS-SN data for asteroids smaller than 30 km and for asteroids larger than 100 km.

time (Table A.4). However, pole orientations for these asteroids remained ambiguous. Clearly, more photometric data are still needed here. Interestingly, the fraction of slowly rotating asteroids is large for these 69 asteroids.

We identified four solutions that were inconsistent with those from DAMIT. Usually, the previous shape modeling was performed over a short interval spanning the rotation period reported in the LCDB database. However, in some cases, either this rotation period was shown to be incorrect or we now prefer a different one (asteroids 1040 and 2962). In two cases, we derived a rotation period that is twice that of DAMIT (asteroids 1461 and 16009).

Within our new shape and spin state solutions, 23 periods are inconsistent with the LCDB periods by more than 5%. Only one has the highest LCDB reliability flag of 3 (asteroid 974). With only one exception (asteroid 1447 Utra), the new periods are larger and typically >100 h. It is not surprising that these cases generally have lower reliability flags and long periods.

In Fig. 10 we show the distribution of rotation periods obtained from ASAS-SN compared to all those available from LCDB. ASAS-SN data are very efficient in identifying longperiod rotators due to the long time span and high cadence of the survey. We discuss this issue in Sect. 4.1. Figure 10 also shows the distribution of pole ecliptic longitudes λ and orbital latitudes β_{orb} for different asteroid sizes, revealing the signatures of YORP in small asteroids. We give more details about this finding in Sect. 4.2. Finally, in Figure 11, we show the distribution of β_{orb} as a function of rotational period. We discuss the implications of our findings for slow rotators in Sect. 4.3.

4. Discussion

ASAS-SN data represent the first sky survey with a fraction of successful shape determinations (15%) exceeding ten percent. This is an order of magnitude improvement over previous efforts based on sparse-in-time datasets. This is partly because of the better photometric accuracy, but also because we limited our analysis to epochs with photometric errors <0.15 mag. The other analyses typically examined a large number of asteroids close to the detection limit. Such data have photometric uncertainties exceeding 0.15 mag. Moreover, information about the uncertainties is often missing, which precludes filtering based on measurement uncertainty. Shape modeling performed on noisy data usually does not provide a unique solution, which decreases the success rate.

We also tested shape modeling with the photometric uncertainty threshold reduced to 0.1 mag. As expected, the resulting dataset contains fewer asteroids and fewer measurements. However, the brighter asteroids are almost unaffected as their measurements usually have accuracy better than 0.1 mag. The faint asteroids are more affected; the photometric accuracy is often in the 0.1–0.15 mag range. Considering the shape modeling results, the two datasets are rather comparable. In general, adding noisier photometry (i.e., using a threshold of 0.15 mag instead of 0.1 mag) resulted in a small number of missed solutions due to the poorer photometric accuracy, but also produced some additional solutions due to the larger number of measurements available for fainter asteroids. We prefer deriving new solutions for fainter asteroids (i.e., threshold of 0.15 mag) rather than confirming more solutions that are already known.

4.1. Excess of slow rotators

Pál et al. (2020) derived 9912 rotation periods using TESS data and found a clear excess of slow ($P \ge 12$ h) rotators compared to existing compilations (their Fig. 7), which suggests these objects were underrepresented in previous ground-based surveys. Similar excesses were also found by Kiss et al. (2019) and Ďurech et al. (2020). This is due to the difficulty of determining long periods using the traditional ground-based observations on which most of the LCDB periods relied (Marciniak et al. 2015, 2018).

Our sample of 920 ASAS-SN periods show an excess of asteroids with periods between ~7 and 24 h (see Fig. 10) when compared to the TESS (Pál et al. 2020) and the LCDB period distributions. We used the most recent version of the LCDB database with 31 280 period estimates, including all the 9912 TESS periods from Pál et al. (2020). Clearly, periods >24 h are not as frequent as in the pure TESS sample. This likely originates in the smaller success rate of shape model determinations for asteroids with these longer periods because the geometry coverage is probably not sufficient. ASAS-SN data seem to be quite useful for deriving shape models and spin states for asteroids with rotation periods of 7–25 h.

We recall that all the currently available rotation period samples are affected by complicated (often unknown or poorly understood) biases. Therefore, these biases should require proper consideration before any more conclusive interpretations are drawn.

4.2. Spin axis anisotropy

The clustering of spin vectors for asteroids smaller than ~ 30 km was already illustrated and explained by Hanuš et al. (2011), and further confirmed in larger datasets (Hanuš et al. 2013a; Ďurech et al. 2016). The thermal forces known as the YORP

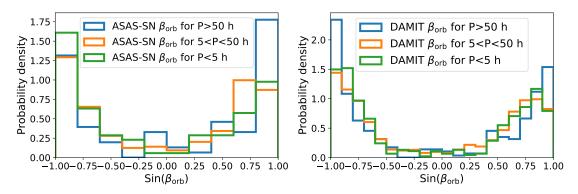


Fig. 11. Distribution of orbital pole latitudes β_{orb} of asteroids with D < 50 km for different rotation period ranges derived from ASAS-SN data (*left*) and from the DAMIT database (*right*).

effect (Bottke et al. 2006; Vokrouhlický et al. 2003) drive a gradual evolution of the spin axis to be perpendicular to the orbital plane. The pole latitudes of the spin axis should cluster near $|\sin\beta_{orb}| = 1$ in our notation. We note that CI provides the pole orientation in the ecliptic coordinate frame (λ , β) and we need to transform it into the orbital frame of the asteroid, where the obliquity of the pole is $\epsilon = 90 - \beta_{orb}$. As the orbital inclinations of typical main-belt asteroids are small ($\leq 20^\circ$), the differences between β and β_{orb} are rather small as well.

We clearly see the latitude clustering in our data for asteroids smaller than 30 km (Fig. 10), where the YORP timescale is shorter than the reorientation timescale due to collisions (Hanuš et al. 2011). Large asteroids (D > 100 km) are not significantly affected by the YORP effect and their pole latitudes are randomly distributed (Fig. 10), as expected for a collisionally dominated population. However, there is a statistically significant excess of prograde rotators ($\beta_{orb} > 0^\circ$) that can be explained by accretion of the pebbles into protoplanets in the prograderotating gaseous disk (Johansen & Lacerda 2010).

Bowell et al. (2014) noted that their distribution of ecliptic longitudes was anisotropic. We see a similar distribution of ecliptic longitudes (Fig. 10) with an excess of asteroids at longitudes of $60-110^{\circ}$. The anisotropy also seems to be present for large asteroids (>100 km, Fig. 10), which suggests it is independent of the size. Interestingly, our latitude distribution for asteroids larger than 100 km is based on 96 solutions, almost half of the whole population (about 200 bodies). The anisotropic distribution of the ecliptic longitudes remains unexplained.

The observed longitude and latitude distributions are affected by observing biases. Hanuš et al. (2011) performed debiassing of these distributions and showed that the debiased latitude distribution for small asteroids is still clearly anisotropic. Moreover, the observation bias in the longitude is negligible, and thus cannot explain the observed anisotropy.

4.3. Spin states of slow rotators

Asteroids having P > 50 h make up a peculiar group, and are not yet fully understood. There are only about 300 such systems in DAMIT and here we have added an additional 45. The general consensus is that these bodies were de-accelerated by the YORP thermal effect (e.g., Čapek & Vokrouhlický 2004; Pravec et al. 2008). This is in agreement with the population being composed only of small asteroids (D < 50 km). Larger asteroids have a Maxwellian distribution of rotation periods consistent with their collisional origin (Pravec et al. 2008). However, alternative theories have also been put forward. For instance, some fragments of disruptive collisions could have slow spin rates or the slow rotation could originate in a synchronous binary that split apart. Moreover, a large fraction of slow rotators are in an excited rotation state, the so-called tumbling mode (Harris & Young 1980; Pravec et al. 2005, 2008). There are two main scenarios proposed for the excitation: YORP spinup eventually self-triggering the tumbling (Vokrouhlický et al. 2007) or YORP spin-up followed by a noncatastrophic collision (Henych & Pravec 2013).

In Fig. 11 we show the pole latitude β_{orb} distributions for three different bins in rotation period, including slow rotators (P > 50 h), for the ASAS-SN solutions and for those in DAMIT. For both datasets the slow rotators have a larger number of poles near $\beta_{\rm orb}$ = ±90° compared to the rest of the population, so there are more spin vectors in the YORP end states. The natural explanation would be that the population of slow rotators is more strongly affected by YORP. It takes more time to slow the period to P > 50 h, and so there is enough time to reach the YORP spin vector end state. A minor complication to this scenario is the presence of secular spin-orbit resonances in which the spin vectors could be temporarily trapped, as in the case of the Koronis family (Slivan 2002; Vokrouhlický et al. 2003). These resonances are likely responsible for the asymmetry in the β_{orb} distribution for asteroids with D < 30 km because they affect only the prograde-rotating asteroids. However, as the excess of spin vectors in the end states of slow rotators is present for both prograde and retrograde bodies, the resonances cannot be the main cause. Another process that acts against the YORP evolution is noncatastrophic collisions. As the slow rotators have a rather small moment of inertia compared to the faster rotators, even a small collision can significantly affect the rotation state. For instance, an impact can change the orientation of the spin axis, the value of rotation period (in both directions) or even excite the rotation. More spin state data combined with dynamical studies should shed more light into the processes that are the most active in shaping the population of slow rotators.

5. Conclusion

We showed that ASAS-SN V-band photometry is a good tool for the physical characterization of asteroids by deriving shapes and rotation properties for 760 asteroids, including 163 new determinations. We validated our results by comparison with determinations based on independent photometric datasets. We also revised incorrect period estimates for several asteroids.

We obtained a statistical sample of asteroid physical properties that was sufficient to confirm and expand on several previously known trends: (i) the underrepresentation of slow rotators in current databases of rotation period estimates (i.e., LCDB) due to observation biases, (ii) the anisotropic distribution of ecliptic pole-latitudes due to nongravitational forces (YORP), and (iii) an anisotropic distribution of ecliptic pole-longitudes of unknown origin.

Most of the successful solutions are for asteroids with more than 200 measurements (Fig. 8), which means that the data cover at least 1500 days (Fig. 3). Clearly, a good coverage of observing geometries is essential for a successful shape model determination. The asteroid also has to be bright enough during the apparition when it has the faintest apparent V-band magnitude (the least convenient geometry, when the asteroid is at aphelion). Asteroids that are too faint at this apparition are likely too faint or have very noisy photometry at the other apparitions.

The newer ASAS-SN *q*-band data will be quite useful for the shape modeling as they are about one magnitude deeper. Apparitions with poor photometric accuracy or brightness at or slightly below our 16.5 mag threshold in this paper will have useful q-band measurements, which could increase the number of successful solutions by a factor of at least 2, particularly since the number of asteroids rises from ~20 000 that reach $V \le 16.5$ mag to ~55000 that reach $V \leq 17.5$ mag. Another benefit of the g-band data is that one-day aliasing will likely be minimized because ASAS-SN now has units at four different longitudes (at least two for everywhere on the sky). Finally, the full potential of ASAS-SN data lies in the possibility of combination with other datasets, as has been done with others surveys in DAMIT.

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Appendix A: Additional tables

Table A.1. Extracted ASAS-SN V-band data.

Number	Name	JD	V mag	V mag unc	CI flag
1	Ceres	2456598.148220	9.009	0.002	1
1	Ceres	2456601.147060	9.151	0.002	1
1	Ceres	2456619.125000	9.306	0.002	1
1	Ceres	2456622.110740	9.189	0.002	1
1	Ceres	2456625.116330	8.933	0.002	1
1	Ceres	2456626.113730	9.029	0.002	1
1	Ceres	2456642.077830	9.117	0.002	1
1	Ceres	2456657.056800	8.865	0.002	1
1	Ceres	2456659.085710	8.914	0.002	1
1	Ceres	2456675.054510	8.859	0.002	1
1000	Piazzia	2455937.957240	17.015	0.205	0
1000	Piazzia	2455999.891650	16.677	0.105	1
1000	Piazzia	2456003.909970	17.154	0.131	1
1000	Piazzia	2456319.039560	15.460	0.059	1
1000	Piazzia	2456326.080760	15.373	0.044	1
1000	Piazzia	2456336.952390	15.010	0.029	1
1000	Piazzia	2456344.986530	15.137	0.041	1
1000	Piazzia	2456354.835490	14.700	0.026	1
1000	Piazzia	2456359.880710	14.484	0.024	1
1000	Piazzia	2456360.887700	14.424	0.024	1
1000	Piazzia	2456371.931610	14.352	0.023	1
1000	Piazzia	2456991.695440	16.886	0.173	0
1000	Piazzia	2457013.694630	16.538	0.201	0
1000	Piazzia	2457183.116350	16.350	0.190	0

Notes. The table provides each asteroid's number and name, the Julian date, the *V*-band magnitude and uncertainty, and a flag indicating whether the data point was used in the light curve inversion (1 for yes, 0 for no). The full table is available at CDS (Strasbourg astronomical Data Center).

Table A.2. Physical properties of asteroids with new shape model determinations based on the V-band ASAS-SN data.

Asteroid		λ_1	$\beta_1 \lambda_2$		β_2	P	М	$N_{\rm A}$	$P_{\rm LCD}$		D
		[deg]	[deg]	[deg]	[deg]	[hours]			[hour	S	[km]
59	Elpis	300	-55			13.6747	CE	289	13.67	3	165.1
70	Panopaea	40	26	233	24	15.8041	С	314	15.81	3	127.9
74	Galatea	109	1	289	14	17.2675	С	327	17.27	3	113.1
83	Beatrix	182	-9			10.1107	Е	351	10.16	3	89.6
105	Artemis	47	24			37.118	С	405	37.15	3	119.0
106	Dione	57	12	237	1	16.2126	С	379	16.21	3	153.4
126	Velleda	120	46	300	32	5.36708	С	249	5.37	3	43.9
131	Vala	58	34	244	17	5.18072	С	368	5.18	3	31.3
133	Cyrene	155	-59	348	-52	12.7086	CE	303	12.71	3	72.2
134	Sophrosyne	100	35	276	7	17.1893	CE	293	17.20	3	112.2
137	Meliboea	173	-7	355	13	25.673	С	316	25.68	3	128.7
139	Juewa	96	-1	271	-25	20.9846	С	279	20.99	3	151.1
140	Siwa	88	-27	265	-27	34.398	CE	320	34.45	3	110.6
168	Sibylla	108	-62			47.015	CE	348	47.01	3	145.4
240	Vanadis	64	12	247	16	10.5606	С	349	10.64	3	87.9
248	Lameia	116	18	292	27	11.9120	С	332	11.91	3	50.1
261	Prymno	150	46	334	34	7.9998	С	327	8.00	3	50.0
326	Tamara	76	7			14.4613	CE	306	14.45	3	89.4

Notes. We provide ecliptic coordinates λ and β of up to two pole solutions, sidereal rotational period *P* (its uncertainty is on the order of the last digit). The method column (M) indicates whether the rotation period was derived by the convex inversion approach (C), the ellipsoid approach (E), or both (CE). The final columns are the number of ASAS-SN measurements N_A , the LCDB period with its reliability flag (Warner et al. 2009), the size *D* from the MP3C database (https://mp3c.oca.eu/catalogue/index.htm), and the DAMIT rotation state solution. The full table is available at the CDS.

Table A.3. Physical properties of asteroids with revised shape model determinations based on the V-band ASAS-SN data and comparison with the DAMIT database.

A	Asteroid	λ ₁ [deg]	β ₁ [deg]	λ ₂ [deg]	β ₂ [deg]	P [hours]	М	N _A	P _{LCD} [hour		D [km]	λ _{D1} [deg]	β _{D1} [deg]	λ _{D2} [deg]	β_{D2} [deg]	P _D [hours]
5	Astraea	84	52	270	44	16.8006	CE	312	16.81	3	108.3	124	39			16.8006
12	Victoria	170	37			8.6604	С	347	8.66	3	115.1	178	-28			8.6603
13	Egeria	34	46			7.04664	С	262	7.04	3	227.0	54	34	233	6	7.04667
16	Psyche	35	-11	215	16	4.19597	С	377	4.20	3	207.2	36	-10			4.19595
17	Thetis	55	12	237	21	12.2660	CE	290	12.27	3	84.9	236	19			12.2660
19	Fortuna	102	51	283	59	7.4432	CE	252	7.44	3	196.4	97	69			7.4432
20	Massalia	122	46	302	47	8.0976	CE	312	8.10	3	131.6	179	39	360	40	8.0990
21	Lutetia	52	-3	232	-0	8.1683	CE	300	8.17	3	108.4	52	-6			8.1683
23	Thalia	340	-70			12.3122	CE	304	12.31	3	106.2	158	-46	343	-74	12.3124
25	Phocaea	342	9			9.9353	CE	334	9.93	3	83.2	347	10			9.9354
28	Bellona	103	-10	282	4	15.7078	CE	362	15.71	3	97.4	98	-10			15.7079

Notes. We provide ecliptic coordinates λ and β of up to two pole solutions, sidereal rotational period *P* (its uncertainty is of the order of the last digit). The method (M) column indicates whether the rotation period was derived by the convex inversion (C), ellipsoid (E) approach, or both (CE) approaches. The final columns are the number of ASAS-SN measurements N_A , the LCDB period with its reliability flag (Warner et al. 2009) and the size *D* from the MP3C database³. The full table is available at the CDS.

Table A.4. Physical properties of asteroids with new rotation period determinations based on the V-band ASAS-SN data.

	Asteroid	P	М	$N_{\rm A}$	D
		[hours]			[km]
835	Olivia	1104.0	С	145	30.4
991	McDonalda	339.5	Е	178	38.6
1034	Mozartia	449.9	Е	216	9.7
1445	Konkolya	59.395	С	96	20.3
1714	Sy	317.8	Е	193	14.0
1745	Ferguson	1078.2	С	136	12.1
1755	Lorbach	7.9765	CE	208	24.9
1787	Chiny	13.5609	Е	173	19.9
1984	Fedynskij	8.1405	Е	187	38.4
2027	Shen Guo	1117.3	Е	164	16.5
2051	Chang	12.0142	CE	183	16.4
2138	Swissair	369.7	С	244	12.9
2158	Tietjen	8.6581	Е	137	22.7
2165	Young	6.39009	CE	143	27.1
2191	Uppsala	31.317	Е	213	17.5
2219	Mannucci	27.460	Е	172	39.1
2226	Cunitza	189.05	Е	159	14.6
2248	Kanda	24.736	Е	169	26.4
2404	Antarctica	2.26238	CE	143	23.2
2405	Welch	14.3411	Е	123	26.4
2413	van de Hulst	211.96	Е	190	20.8
2475	Semenov	12.2370	Е	131	14.5
2502	Nummela	14.3151	Е	97	19.0
2660	Wasserman	628.3	Е	137	9.2
2780	Monnig	681.8	Е	91	4.8
2795	Lepage	40.368	E	107	6.1
2819	Ensor	161.66	Е	130	9.7
2837	Griboedov	3.94988	С	119	12.3

Notes. We provide the sidereal rotational period P (its uncertainty is on the order of the last digit). The method column (M) indicates whether the rotation period was derived by the convex inversion approach (C), the ellipsoid approach (E), or both (CE). The final two columns are the number of ASAS-SN measurements N_A and the size D from the MP3C database. The full table is available at the CDS.