

Clear all symbols from previous evaluations to avoid problems

```
Clear["Global`*"]
```

Clusters on a one-dimensional lattice

Count cluster sizes on a one-dimensional lattice and save *cluster numbers* (probability, normalized per site, of finding a cluster of a certain size in a lattice) into the array *clusters*

```
In[1]:= n = 1000; (* lattice size *)
np = 100; (* number of probabilities *)
nconf = 500; (* number of configurations generated for each probability *)
probs = N[Range[np] / np];
ns = ConstantArray[0.0, {np, n}];
Do[ (* loop over probabilities *)
  Do[ (* loop over configurations *)
    lattice = Array[If[RandomReal[] <= probs[[ip]], 1, 0] &, n];
    s = 0;
    Do[ (* loop over lattice *)
      If[lattice[[i]] == 1,
        s++,
        If[s > 0,
          ns[[ip, s]]++;
          s = 0
        ]
      ],
      {i, 1, n}
    ];
    If[s > 0, ns[[ip, s]]++],
    {ic, 1, nconf}
  ],
  {ip, 1, np}
];
ns = ns / nconf / n;
```

Check that approximately

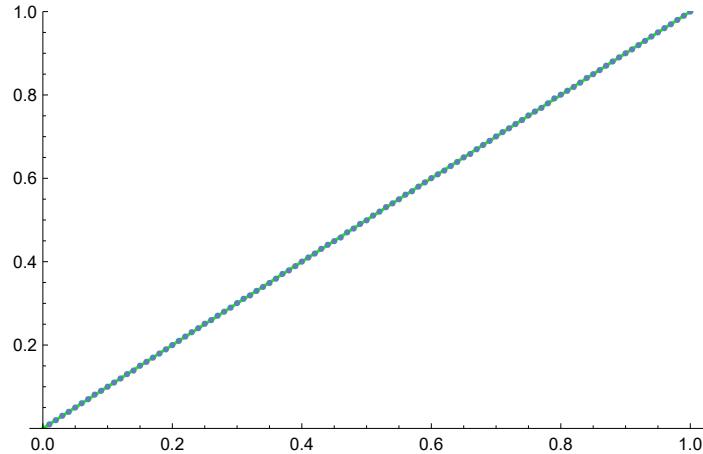
$$M_1(p) = \sum_s n_s(p) s = p$$

and that the average cluster size at a randomly chosen site

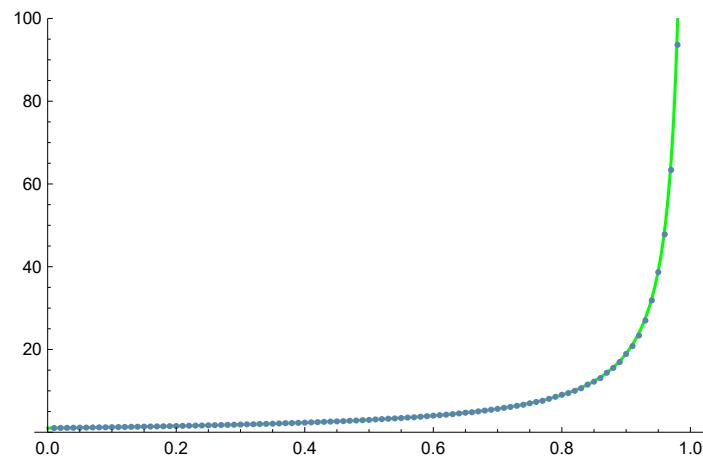
$$S = \frac{M_2(p)}{M_1(p)} = \frac{1+p}{1-p} \quad \text{where} \quad M_2(p) = \sum_s n_s(p) s^2$$

```
In[8]:= moment1 = ConstantArray[0.0, np];
moment2 = ConstantArray[0.0, np];
S = ConstantArray[0.0, np];
Do[ (* loop over probabilities *)
  Do[ (* loop over configurations *)
    moment1[[ip]] += ns[[ip, s]] * s;
    moment2[[ip]] += ns[[ip, s]] * s^2,
    {s, 1, n}
  ];
  S[[ip]] = moment2[[ip]] / moment1[[ip]],
  {ip, 1, np}
];
Show[{Plot[p, {p, 0, 1}, PlotRange -> {0, 1}, PlotStyle -> Green],
ListPlot[Transpose[{probs, moment1}]]}]
Show[{Plot[(1+p)/(1-p), {p, 0, 1}, PlotRange -> {0, 100}, PlotStyle -> Green],
ListPlot[Transpose[{probs, S}]]}]
```

Out[12]=



Out[13]=



Comparison of cluster numbers with theoretical prediction

```
In[19]:= fns[p_, s_] := p^s (1 - p)^2;
smin = 1; smax = 5;
pexact =
  Plot[Table[fns[p, s], {s, smin, smax}], {p, 0, 1}, PlotRange -> All, PlotStyle -> Green];
pMC = ListPlot[Table[Transpose[{probs, ns[[All, s]]}], {s, smin, smax}],
  PlotRange -> All, PlotStyle -> PointSize[0.01]];
Show[pexact, pMC]
```

Out[23]=

