

Clear all symbols from previous evaluations to avoid problems

```
In[19]:= Clear["Global`*"]
```

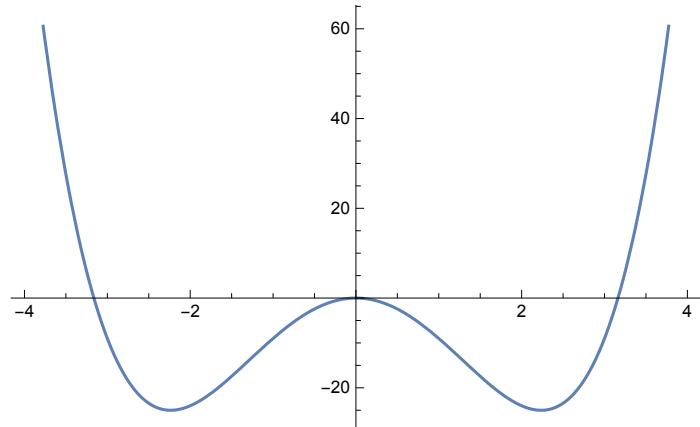
## Find a minimum of a given function

1D function

```
In[20]:= g[x_] := x^4 - 10 x^2;
Solve[D[g[x], x] == 0, x]
```

```
Out[21]= { {x → 0}, {x → -Sqrt[5]}, {x → Sqrt[5]} }
```

```
In[22]:= f[x_] := x[[1]]^4 - 10 x[[1]]^2;
Plot[f[{x}], {x, -4, 4}]
{point, value, niter} = MyMinimization[{0.0}, {-0.2}, f, 10^(-10)]
N[{Sqrt[5], g[Sqrt[5]]}]
```



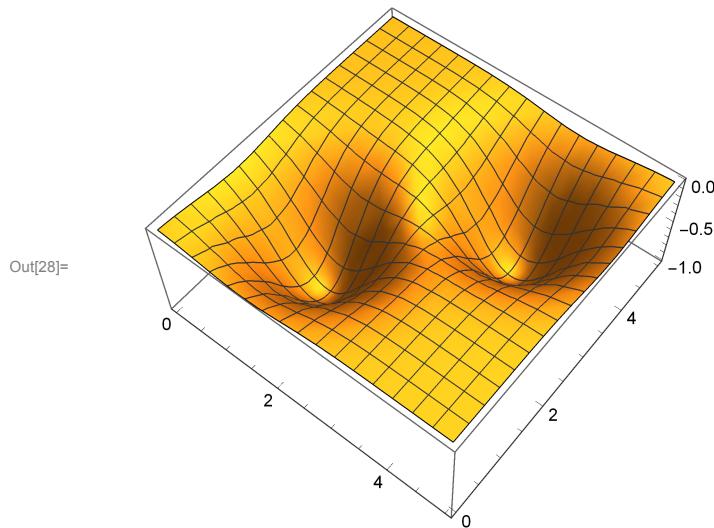
```
Out[24]= { {-2.236071777}, -25., 38}
```

```
Out[25]= {2.236067977, -25.}
```

```
In[26]:= {point, value, niter} // InputForm
```

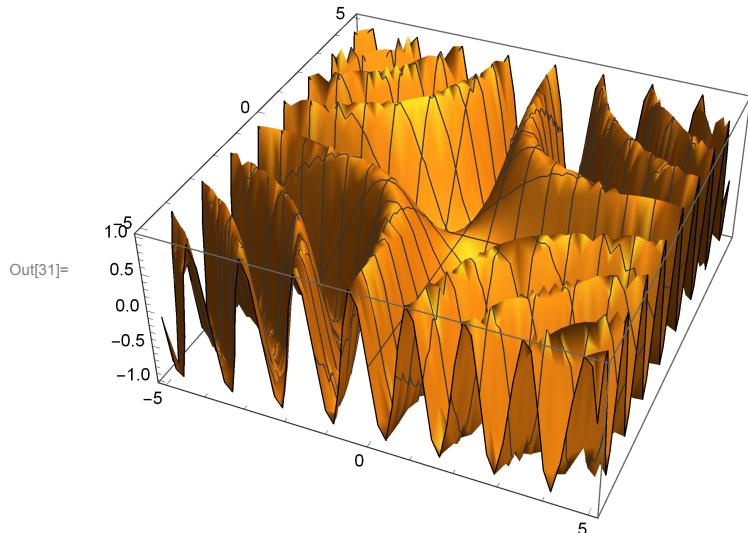
```
Out[26]//InputForm=
{ {-2.236071777343761}, -24.9999999971122, 38}
```

```
In[27]:= f[x_] := Module[
  {n, i},
  n = Length[x];
  Return[
    -Exp[-Sum[(x[[i]] - 1.5)^2, {i, 1, n}]] - Exp[-Sum[(x[[i]] - 3.5)^2, {i, 1, n}]]]
  ];
Plot3D[f[{x, y}], {x, 0, 5}, {y, 0, 5}]
```



```
In[29]:= {point, value, niter} = MyMinimization[{4.5, 0.5}, {0.01, 0.01}, f, 10^(-10)]
Out[29]= {{1.500676019, 1.500678098}, -1.000336367, 114}
```

```
In[30]:= f[x_] := Module[
  {n, i},
  n = Length[x];
  Return[Sin[x[[1]] * x[[2]]]]
];
Plot3D[f[{x, y}], {x, -5, 5}, {y, -5, 5}]
```



```
In[32]:= {point, value, niter} = MyMinimization[{0.5, 0.1}, {0.1, 0.1}, f, 10^(-8)]
Out[32]= {{1.355838185, -1.158516446}, -0.9999999994, 50}
```

## Nonlinear least-square fitting

Fitting a function with noise

```
In[33]:= myf[x_, p1_, p2_, p3_] := p1 * Exp[-p2 * (x - p3)^2];
n = 40;
d = 0.1;
grid = Table[0.0 + i * 0.1, {i, 1, n}];
data = Table[myf[grid[[i]], 2.0, 2.0, 2.0] + RandomReal[{-d, d}], {i, 1, n}];

In[38]:= f[par_] := Module[
  {i, fx, squares},
  squares = 0.0;
  Do[
    fx = myf[grid[[i]], par[[1]], par[[2]], par[[3]]] - data[[i]];
    squares += fx * fx,
    {i, 1, n}
  ];
  Return[squares]
];
{point, value, niter} = MyMinimization[{2.0, 2.0, 2.0}, {0.01, 0.01, 0.01}, f, 10^(-8)]
{point, value, niter} = MyMinimization[{0.0, 0.0, 1.0}, {1.0, 1.0, 1.0}, f, 10^(-8)]

Out[39]= {{2.006715073, 1.937825346, 2.002613654}, 0.1157463412, 95}

Out[40]= {{2.006716956, 1.937840457, 2.002613066}, 0.1157463409, 144}

In[41]:= data2 = Table[myf[grid[[i]], 2.0, 2.0, 2.0], {i, 1, n}];
data3 = Table[myf[grid[[i]], Delete[point, 0]], {i, 1, n}];
ListPlot[{Transpose[{grid, data}], Transpose[{grid, data2}],
  Transpose[{grid, data3}]}, Joined → {False, True, True}]
```

