

Astrophysics of gravitational wave sources

Lecture 7: Common envelope & chemically-homogeneous evolution

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Logarithmic change of the Roche lobe radius with orbital angular momentum and total mass fixed:

$$R'_L \equiv \frac{d \log R_L}{d \log M_1} = (1 + q) \cdot \left(\frac{d \log R_L/a}{d \log q} + \frac{d \log a}{d \log q} \right) \\ \approx 2.13q - 1.67, \quad 0 < q \lesssim 50;$$

Polytrope with $\gamma = 5/3$ has adiabatic $R \sim M^{-1/3}$, which leads to critical q

Dynamical instability -> total energy
conserved

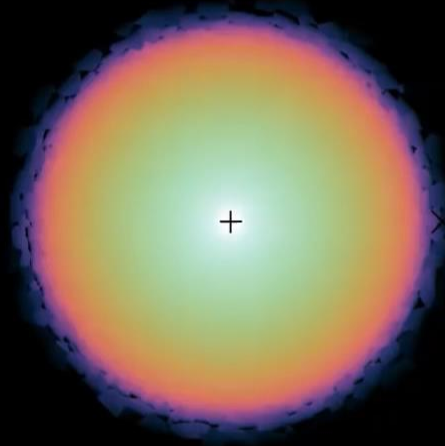
(Eggleton's book)

Calculation of energy balance

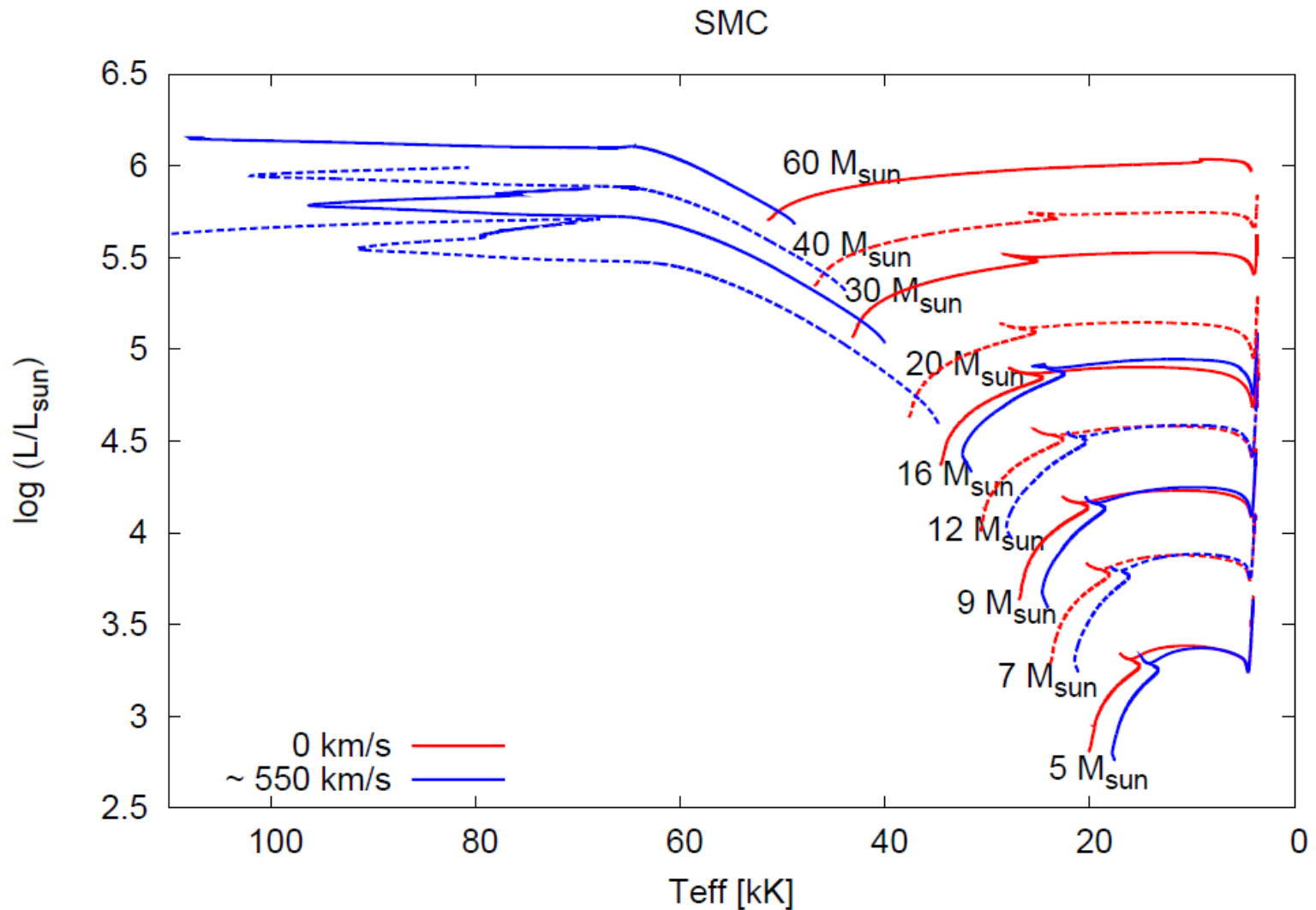
$100R_{\odot}$

$t = 0.00 \text{ d}$

- Common envelope simulation lasts \sim few orbital periods
- Unbinds only $\sim 8\%$ of the envelope, although expected to unbind everything



Chemically-homogeneous evolution



Brotts et al. (2011)

Why do homogeneous stars evolve bluewards?

$$R \propto \mu^{2/3} M^{0.81} \quad \text{with homology relation and CNO cycle}$$

$$L \propto \frac{\mu^{7.5} M^{5.5}}{R^{0.5}} \quad \text{with homology relation and Kramer's opacity law}$$



$$T_{\text{eff}} \propto \mu^{1.5} M^{0.75}$$