Astrophysics of gravitational wave sources Lecture 5: White dwarfs, neutron stars, black holes

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Chandrasekhar mass

- [hbar] = erg s = g cm^2 s^-1
- [c] = cm/s
- [P] = cm^2/s^2 g/cm^3 = g s^-2 cm^-1
- For gamma=4/3 polytrope (P=K rho^gamma): M ~ (K/G)^1.5
- The units on K: we'll put in mp... mass of proton, combine with hbar and c (baryons contribute all of the mass)

- M_Chandrasekhar = (hbar c/G)^1.5 / (mu mp)^2 ~ m_planck^3/mp^2
- Electron mass does not appear in the equation!

ns.pdf



A. Heger website 2sn.org

$1 \text{ erg} = 10^{-7} \text{ J}$

Massive star death





 $M_{\rm initial}$ > 8 M $_{\odot}$ Collapse from WD size ~0.3s



Proto-neutron star ~60 km Binding energy ~ 3×10^{53} ergs

Reason not fully understood



All NS binding energy released before 10-100s





Stalled shock at 100-200 km Neutrino cooling ~ 10⁵² ergs/s Duration up to ~1 s

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Explosion energy ~10<sup>51</sup> ergs
10<sup>-3</sup> – 10<sup>-1</sup> M<sub>☉</sub> of Nickel-56
Shock at surface in ~hours
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Collapse of the core

$$(A, Z) + e^- \rightarrow (A, Z - 1) + \nu_e,$$

$$\epsilon_F \ge M(A, Z - 1) - M(A, Z) \qquad \epsilon_F = \sqrt{(p_F c)^2 + (m_e c^2)^2}$$

 $M(A', Z') \to M(A' - 1, Z') + n$ "neutron drip,"

$$\rho_{\rm nuc}\approx 2.8\times 10^{14}\,{\rm g\,cm^{-3}}$$