

# Astrophysics of gravitational wave sources

Lecture 4: Single star evolution

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# Why do stars shine?

(wrong answers only)

# Two-point boundary value problem

$$\frac{dP}{dM_r} = -\frac{GM_r}{4\pi r^4},$$

$$\frac{dr}{dM_r} = \frac{1}{4\pi r^2 \rho},$$

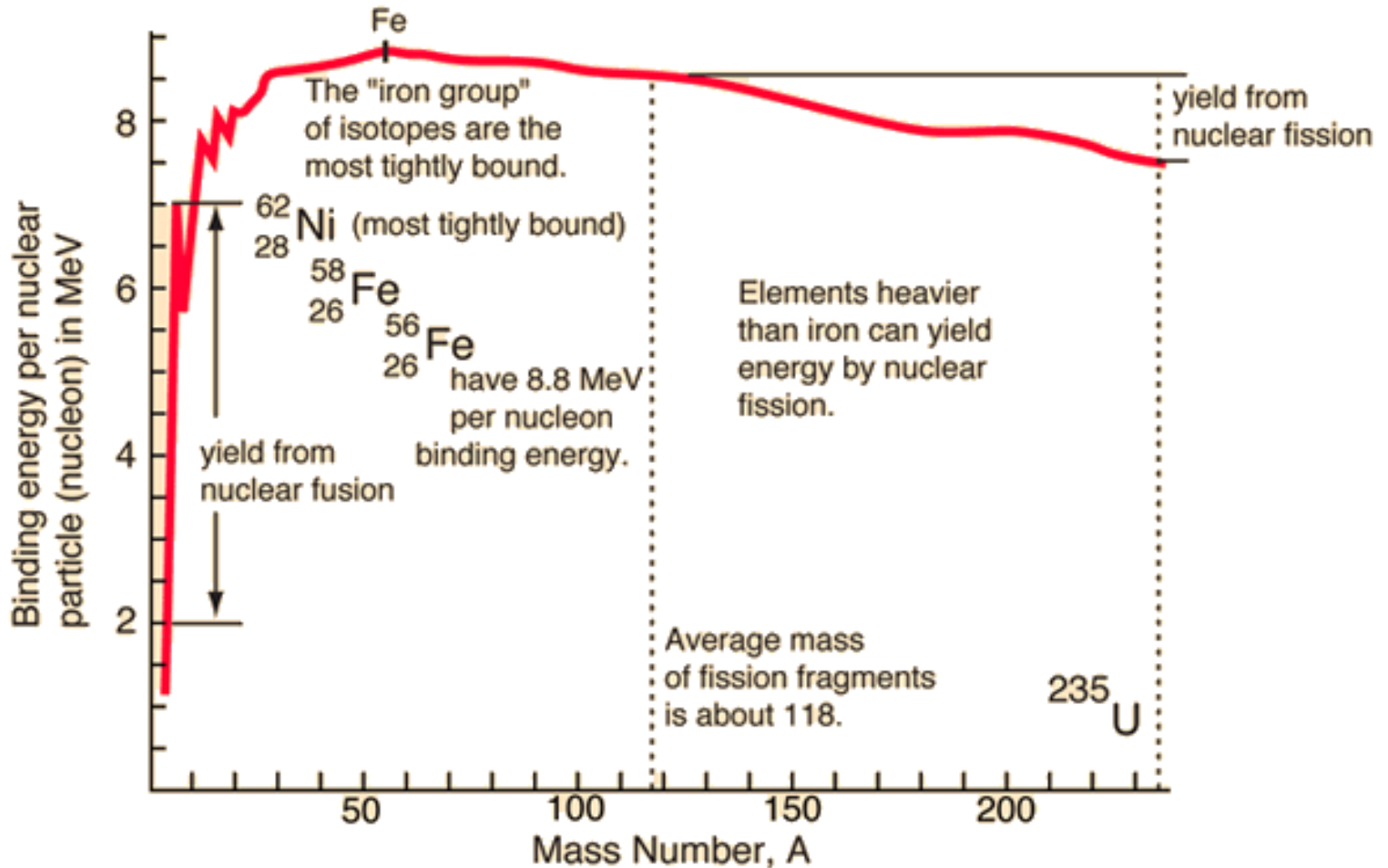
$$\frac{dT}{dM_r} = -\frac{3\kappa L_r}{64\pi^2 acT^3 r^4}, \quad \text{but convection!}$$

$$\frac{dL_r}{dM_r} = \epsilon.$$

# Separation of stellar timescales

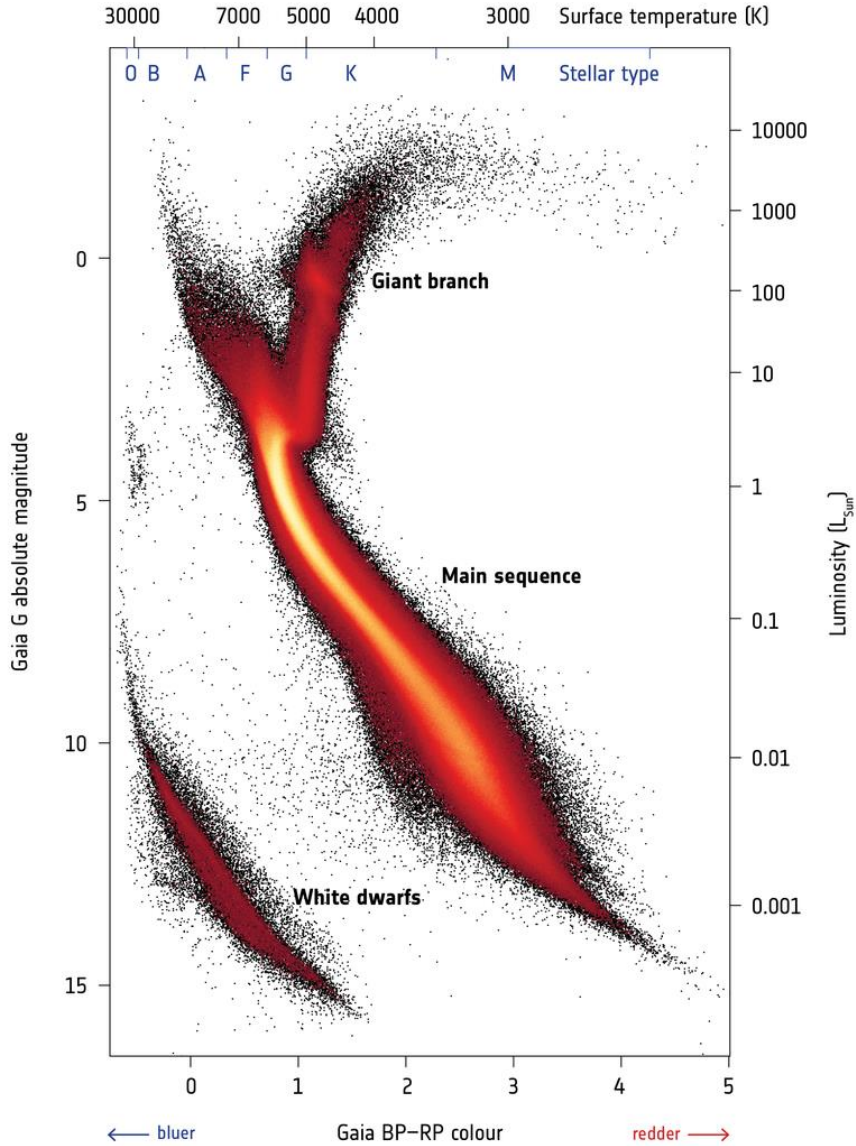
- Dynamical (free-fall, sound-crossing) timescale
- (Viscous timescale)
- Thermal (Kelvin-Helmholtz) timescale
- Nuclear timescale

# Why do stars evolve?

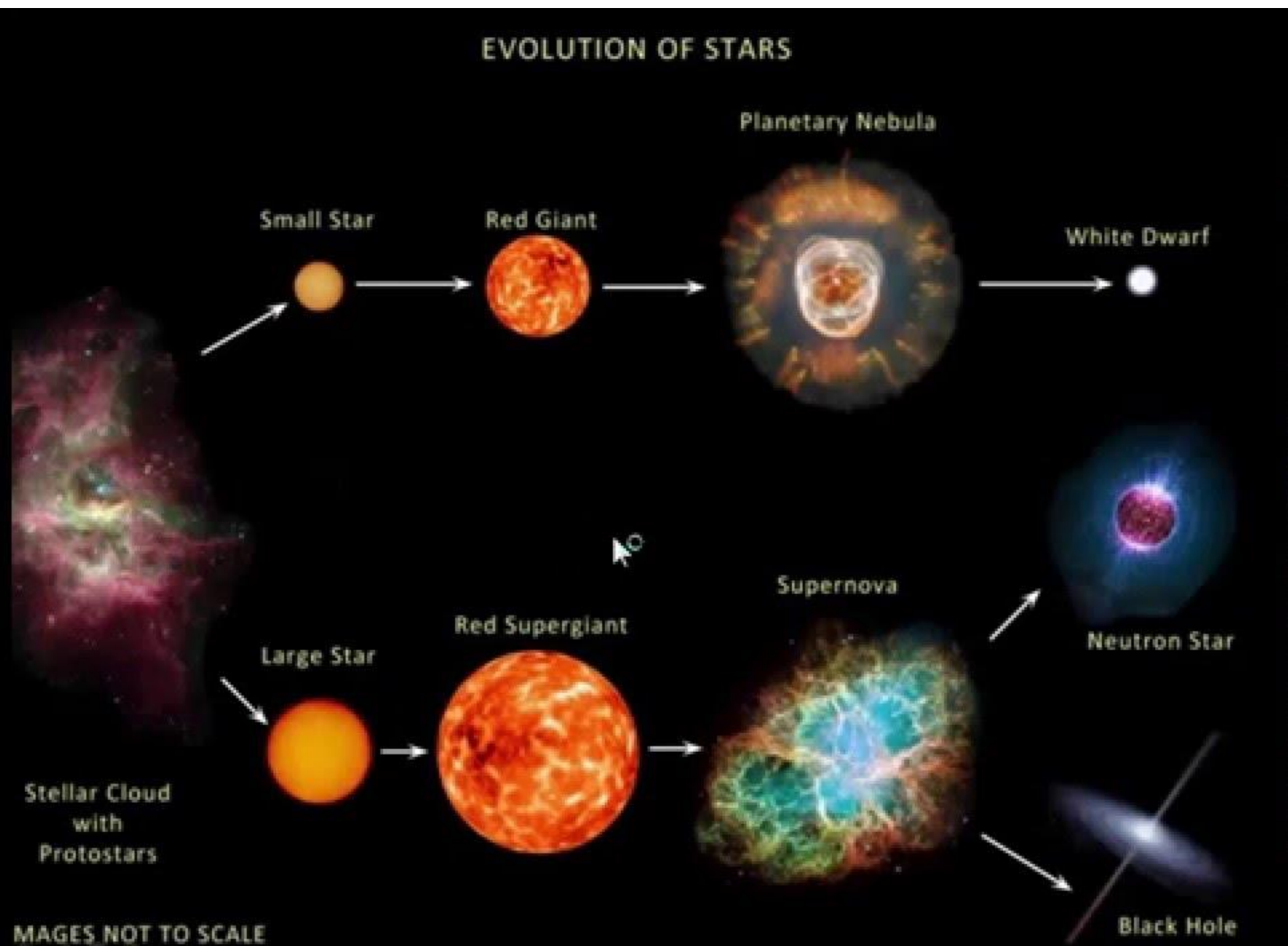


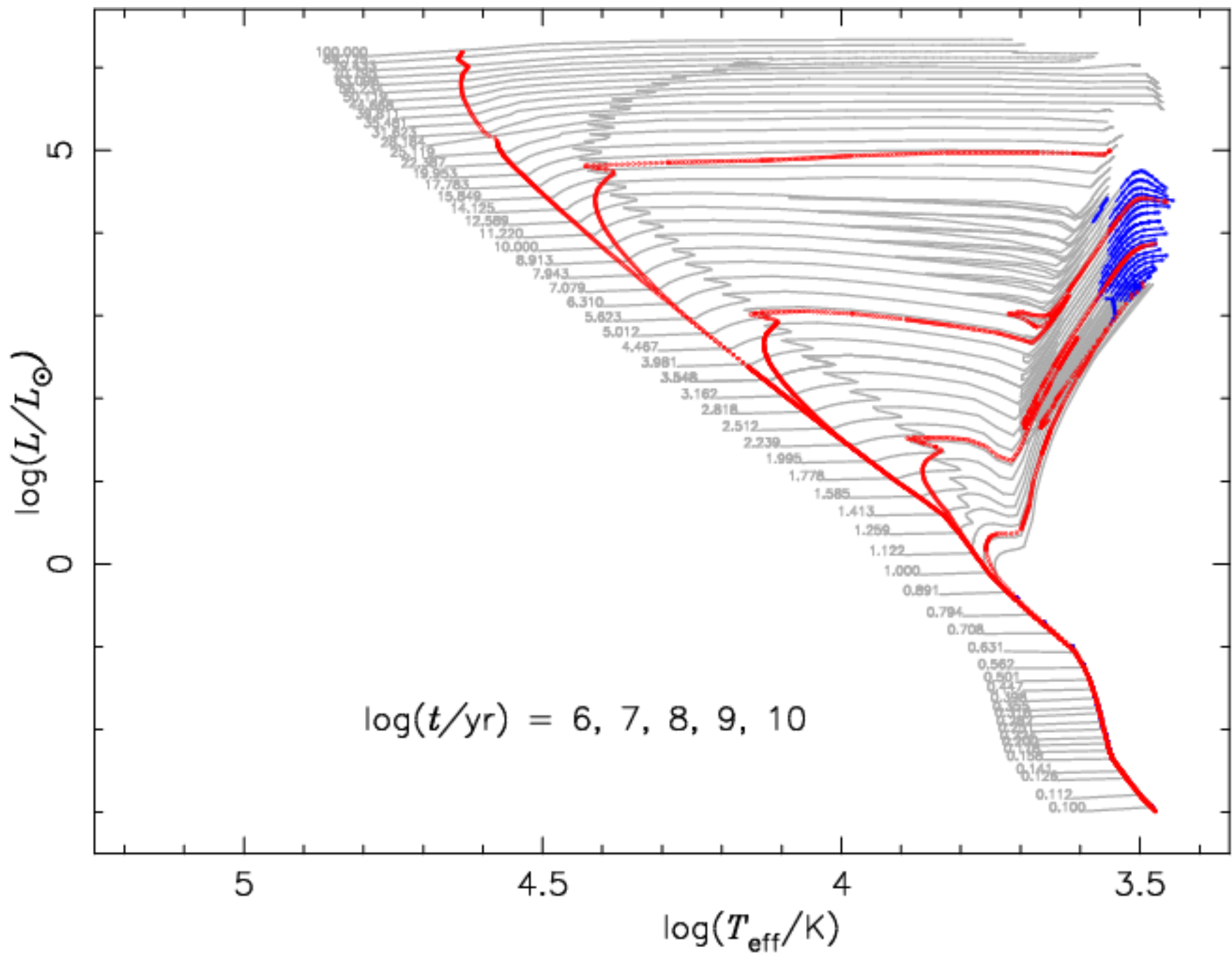
# Main parameters of stars

## → GAIA'S HERTZSPRUNG-RUSSELL DIAGRAM



# Stellar evolution

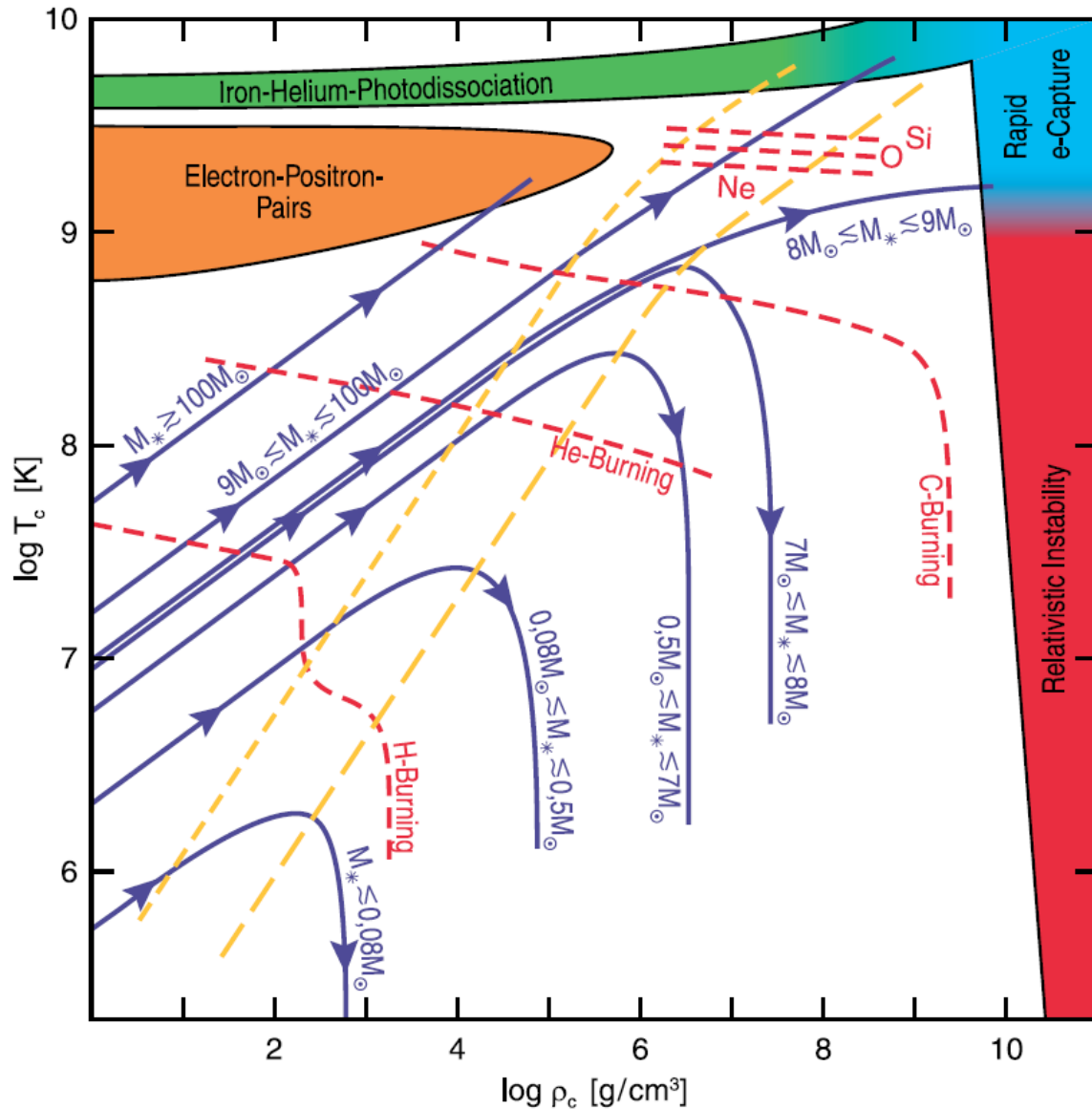






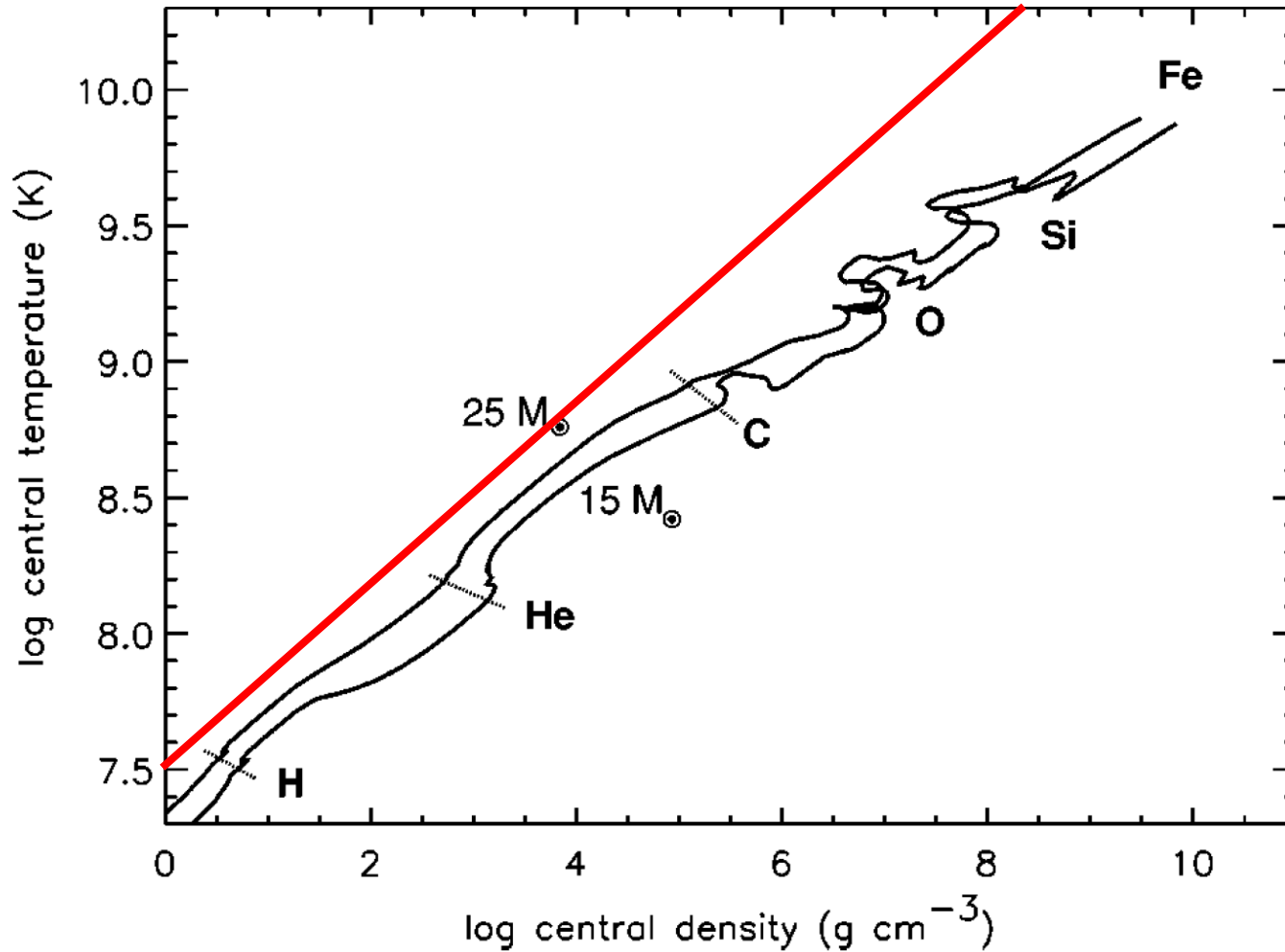
# Single star evolution before core-collapse

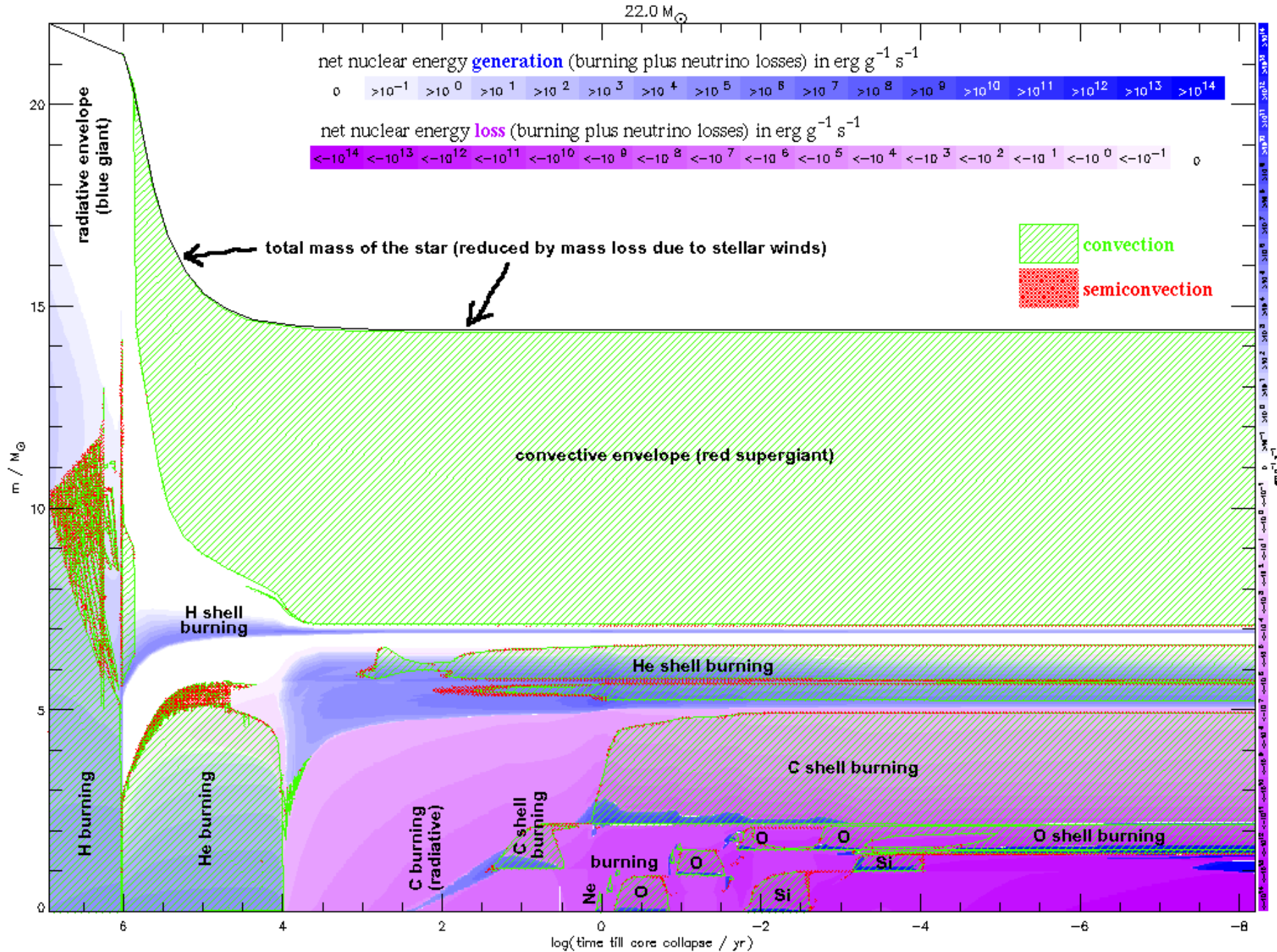
Central temperature and pressure



# Single star evolution before core-collapse

Central temperature and pressure





A. Heger website 2sn.org

# Physical processes inside massive star

- Neutrino losses
  - Mostly due to thermal processes ( $T^9$ ), later due to neutronization ( $T^6$ )
  - Accelerates evolution ( $\sim$ day timescale for silicon)
- Convection
  - Mixing length theory, but convective and nuclear timescales comparable
  - Mixing as a diffusive process
- Semi-convection
  - Schwarzschild – instability only due to temperature/pressure gradients
  - Ledoux – also takes into account chemical composition
  - Unstable by Schwarzschild & stable by Ledoux = semi-convection
  - Diffusion coefficient uncertain
- Overshoot mixing
  - Modeled by diffusion
- Rotation & magnetic fields
  - Coupling of core to envelope – affected by mass loss
- Mass loss

